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## Squares and Square roots

Ex - 6.1

Q1. What will be the unit digit of the squares of the following numbers:-

(i) ~~81~~ \* We know that if a number has its unit's place digit as  $a$ , then its square will end with the unit digit of the multiplication  $a \times a$ .

(i) 81

Since the given number has its unit's place digit as 1, its square will end with the unit digit of the multiplication  $= 1 \times 1 = 1$ .

(ii) 272

Since the given number has its unit's place digit as 2, its square will end with the unit digit of the multiplication  $= 2 \times 2 = 4$ .

(iii) 799

Since the given number has its unit's place digit as 9, its square will end with the unit digit of the multiplication  $= 9 \times 9 = 81$ , Ans 1.

(iv) 3853

Since the given number has its unit's place digit as 3, its square will end with the unit digit of the multiplication  $= 3 \times 3 = 9$ .

(iv) 1234

Since the given number has its unit's place digit as 4, its square will end with the unit digit of the multiplication  $= 4 \times 4 = 16 = 6$  Ans

(v) 26387

Since the given number has its unit's place digit as 7, its square will end with the unit digit of the multiplication  $= 7 \times 7 = 49 = 9$  Ans

(vi) 52698

Since the given number has its unit's place digit as 8, its square will end with the unit digit of the multiplication  $= 8 \times 8 = 64 = 4$  Ans

(vii) 99880

Since the given number has its unit's place digit as 0, its square will end with the unit digit of the multiplication  $= 0 \times 0 = 0$  Ans

(ix) 12796

Since the given number has its unit's place digit as 6, its square will end with the unit digit of the multiplication  $= 6 \times 6 = 36 = 6$  Ans

(x) 55555

Since the given number has its unit's place digit as 5, its square will end with the unit digit of the multiplication  $= 5 \times 5 = 25 = 5$  Ans

Q2. The following numbers are obviously not perfect squares. Give reason.

$$1^2 = 1, 2^2 = 4, 3^2 = 9, 4^2 = 16, 5^2 = 25$$

$$6^2 = 36, 7^2 = 49, 8^2 = 64, 9^2 = 81$$

Perfect square no. [1, 4, 9, 6, 5, ...] [0, 2, 3, 7, 8 - Not perfect square no.]

- (i) 1057 ends with 7 at unit place. So it is not a perfect square number.
- (ii) 23453 ends with 3 at unit place. So it is not a perfect square number.
- (iii) 7928 ends with 8 at unit place. So it is not a perfect square number.
- (iv) 2, 22, 222 ends with 2 at unit place. So it is not a perfect square number.
- (v) 64000 ends with 3 zeros. So it cannot a perfect square number.
- (vi) 89722 ends with 2 at unit place. So it is not a perfect square number.
- (vii) 22000 ends with 3 zeros. So it cannot a perfect square number.
- (viii) 505050 ends with 1 zero. So it is not a perfect square number.

Q3. The squares of which of the following would be odd numbers?

\* We know that the square of an odd number is odd and the square of an even number is even.

(i) 431 - The square of 431 is an odd number.

(ii) 2826 → The square of 2826 is an even number.

(iii) 7779 → The square of 7779 is an odd number.

(iv) 82004 → The square of 82004 is an even number.

Ans (i) and (iii)

Q4. Observe the following pattern and find the missing digits :-

$$11^2 = 121$$

$$101^2 = 10201$$

$$1001^2 = 1002001$$

$$100001^2 = \underline{10000} \quad \underline{20000} \quad \underline{1}$$

$$10000001^2 = \underline{10000000} \quad \underline{20000000} \quad \underline{1}$$

Q5. Observe the following pattern and supply the missing numbers:-

$$11^2 = 121$$

$$101^2 = 10201$$

$$10101^2 = 102030201$$

$$1010101^2 = \underline{1020304030201}$$

$$\underline{101010101^2 = 10203040504030201}$$

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Q6. Using the given pattern, find the missing numbers:-

$$1^2 + 2^2 + 2^2 = 3^2$$

$$2^2 + 3^2 + 6^2 = 7^2$$

$$3^2 + 4^2 + 12^2 = 13^2$$

$$4^2 + 5^2 + 20^2 = 21^2$$

$$5^2 + 6^2 + 30^2 = 31^2$$

$$6^2 + 7^2 + 42^2 = 43^2$$

Q7. Without adding, find the sum:-

We know that the sum of  $n$  odd numbers  $= n^2$

(i)  $1 + 3 + 5 + 7 + 9$

Sol. Sum of 1<sup>st</sup> 5 odd number.  $= (5)^2$   
 $= 25$

(ii)  $1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19$

Sum of 1<sup>st</sup> 10 odd number  $= (10)^2$   
 $= 100$

(iii)  $1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21 + 23$

Sum of 1<sup>st</sup> 12 odd number  $= (12)^2$   
 $= 144$

Q8. (i) Express 49 as the sum of 7 odd numbers.

Sol. We know, sum of 1<sup>st</sup>  $n$  odd natural numbers is  $n^2$

So  $49 = 7^2$

$49 =$  Sum of 1<sup>st</sup> 7 odd natural numbers  
 $1 + 3 + 5 + 7 + 9 + 11 + 13$

Q. Express 121 as the sum of 11 odd numbers.

Sol. We know, sum of first  $n$  odd natural numbers is  $n^2$ . So  $121 = 11^2$

$121 =$  sum of 11 odd natural numbers

$$1 + 3 + 5 + 7 + 9 + 11 + 13 + 15 + 17 + 19 + 21$$

Q. How many numbers lie between squares of the following numbers?

(i) ~~12 and 13~~

\* We know that numbers between  $n^2$  and  $(n+1)^2 = 2n$ .

(i) 12 and 13

Numbers between  $12^2$  and  $(12+1)^2 = 2 \times 12$   
 $\Rightarrow 24$

(ii) 25 and 26

Numbers between  $25^2$  and  $(25+1)^2 = 2 \times 25$   
 $\Rightarrow 50$

(iii) 99 and 100

Numbers between  $99^2$  and  $100^2 \Rightarrow 2 \times 99$   
 $\Rightarrow 198$

Ex-6.2

Q1. Find the squares of the following numbers:-

(i) 32

$$32 = (30 + 2)^2$$

$$\therefore (a+b)^2 = a^2 + 2ab + b^2$$

$$(30+2)^2 \Rightarrow (30)^2 + 2 \times 30 \times 2 + (2)^2$$

$$\Rightarrow 900 + 120 + 4$$

$$\Rightarrow 1024$$

$$(32)^2 = \underline{1024} \text{ Ans}$$

(ii) 35 = (30 + 5)<sup>2</sup>

$$\text{Sol: } (30+5)^2 = (30)^2 + 2 \times 30 \times 5 + (5)^2$$

$$\Rightarrow 900 + 300 + 25$$

$$(35)^2 = \underline{1225} \text{ Ans}$$

(iii) 86 = (80 + 6)<sup>2</sup>

$$(80+6)^2 = (80)^2 + 2 \times 80 \times 6 + (6)^2$$

$$\Rightarrow 6400 + 960 + 36$$

$$(86)^2 = \underline{7396} \text{ Ans}$$

(iv) 93 = (90 + 3)<sup>2</sup>

$$(90+3)^2 = (90)^2 + 2 \times 90 \times 3 + (3)^2$$

$$\Rightarrow 8100 + \cancel{540} + 9$$

$$(93)^2 = \underline{8649} \text{ Ans}$$

(v) 71 = (70 + 1)<sup>2</sup>

$$(70+1)^2 \Rightarrow (70)^2 + 2 \times 70 \times 1 + (1)^2$$

$$\Rightarrow 4900 + 140 + 1$$

$$(71)^2 = \underline{5041} \text{ Ans}$$



$$(vi). 46 = (40+6)^2.$$

$$\text{Sol. } (40+6)^2 = (40)^2 + 2 \times 40 \times 6 + (6)^2$$

$$(46)^2 \Rightarrow 1600 + 480 + 36$$

$$\Rightarrow 2116 \text{ Ans}$$

Q2: Write a Pythagoras triplet whose one member is:-

\* For any natural number  $m > 1$ ,  $2m$ ,  $m^2 - 1$ ,  $m^2 + 1$  forms a Pythagoras triplet.

(i) 6

$$\text{Sol. } 2m = 6$$

$$m = \frac{6}{2} = 3$$

$$m^2 - 1$$

$$(3)^2 - 1 = 9 - 1 = 8.$$

$$m^2 + 1$$

$$(3)^2 + 1 = 9 + 1 = 10$$

$(6, 8, 10)$  is a Pythagoras triplet.

(ii) 14

$$2m = 14$$

$$m = \frac{14}{2} = 7$$

$$m^2 - 1$$

$$(7)^2 - 1 = 49 - 1 = 48$$

$$m^2 + 1$$

$$(7)^2 + 1 = 49 + 1 = 50$$

$(14, 48, 50)$  is a Pythagoras triplet.

iii)

16

Sol.

$$2m = 16$$

$$m = \frac{16}{2} = 8$$

$$m^2 - 1$$

$$(8)^2 - 1$$

$$64 - 1 = 63$$

$$m^2 + 1$$

$$(8)^2 + 1$$

$$64 + 1 = 65$$

(16, 63, 65) is a pythagorean triplet.

iv)

18

Sol.

$$2m = 18$$

$$m = \frac{18}{2} = 9$$

$$m^2 - 1$$

$$(9)^2 - 1$$

$$81 - 1 = 80$$

$$m^2 + 1$$

$$(9)^2 + 1$$

$$81 + 1 = 82$$

(18, 80, 82) is a pythagorean triplet.

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Ex-6.3

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Q1. What could be the possible one's digits of the square root of each of the following numbers?

(i) 9801

$$1^2 = 1$$

$$2^2 = 4$$

$$3^2 = 9$$

$$4^2 = 16$$

$$5^2 = 25$$

$$6^2 = 36$$

$$7^2 = 49$$

$$8^2 = 64$$

$$9^2 = 81$$

$$10^2 = 100$$

As one's digit in the square root of 9801 may be 1 or 9.

(ii) 99856

As one's digit in the square root of 99856 may be 4 or 6.

(iii) 998001

As one's digit in the square root of 998001 may be 1 or 9.

(iv) 657666025

As one's digit in the square root of 657666025 may be 5.

Q2. Without doing any calculation, find the numbers which are surely not perfect squares.

\* We know that the numbers ending with 2, 3, 7 or 8 are not perfect squares.

- (i) 153  $\rightarrow$  Ending with 3.
- (ii) 257  $\rightarrow$  Ending with 7
- (iii) 408  $\rightarrow$  Ending with 8
- (iv) 441  $\rightarrow$  Ending with 1, So it is a perfect square number.

(i), (ii) and (iii) are not perfect squares because they ended with 3, 7 and 8.

Ex 6.3 Class 8 Maths Question 3.

Find the square roots of 100 and 169 by the method of repeated subtraction.

Solution:

Using the method of repeated subtraction of consecutive odd numbers, we have

$$(i) \begin{aligned} 100 - 1 &= 99, 99 - 3 = 96, 96 - 5 = 91, 91 - 7 = 84, \\ 84 - 9 &= 75, 75 - 11 = 64, 64 - 13 = 51, \\ 51 - 15 &= 36, 36 - 17 = 19, 19 - 19 = 0 \end{aligned}$$

(Ten times repetition)

Thus  $\sqrt{100} = 10$

(ii)  $169 - 1 = 168$ ,  $168 - 3 = 165$ ,  $165 - 5 = 160$ ,  
 $160 - 7 = 153$ ,  $153 - 9 = 144$ ,  $144 - 11 = 133$ ,  
 $133 - 13 = 120$ ,  $120 - 15 = 105$ ,  $105 - 17 = 88$ ,  
 $88 - 19 = 69$ ,  $69 - 21 = 48$ ,  $48 - 23 = 25$ ,  
 $25 - 25 = 0$

(Thirteen times repetition)

Thus  $\sqrt{169} = 13$

### Ex 6.3 Class 8 Maths Question 4.

Find the square roots of the following numbers by the Prime Factorisation Method :

(i) 729

(ii) 400

(iii) 1764

(iv) 4096

(v) 7744

(vi) 9604

(vii) 6929

(viii) 9216

(ix) 529

(x) 8100

#### Solution:

(i) By prime factorisation, we get  
 $729 = \underline{3 \times 3} \times \underline{3 \times 3} \times \underline{3 \times 3}$   
 $\therefore \sqrt{729} = 3 \times 3 \times 3$   
 $= 27$

3	729
3	243
3	81
3	27
3	9
3	3
	1

(ii) By prime factorisation, we get  
 $400 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{5 \times 5}$   
 $\therefore \sqrt{400} = 2 \times 2 \times 5$   
 $= 20$

2	400
2	200
2	100
2	50
5	25
5	5
	1

(iii) By prime factorisation, we get  
 $1764 = \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{7 \times 7}$   
 $\therefore \sqrt{1764} = 2 \times 3 \times 7$   
 $= 42$

2	1764
2	882
3	441
3	147
7	49
7	7
	1

(iv) By prime factorisation, we get  
 $4096 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2}$   
 $\times \underline{2 \times 2} \times \underline{2 \times 2}$   
 $\therefore \sqrt{4096} = 2 \times 2 \times 2 \times 2 \times 2 \times 2$   
 $= 64$

2	4096
2	2048
2	1024
2	512
2	256
2	128
2	64
2	32
2	16
2	8
2	4
2	2
	1

(v) By prime factorisation, we get  
 $7744 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{11 \times 11}$   
 $\therefore \sqrt{7744} = 2 \times 2 \times 2 \times 11$   
 $= 88$

2	7744
2	3872
2	1936
2	968
2	484
2	242
11	121
11	11
	1

(vi) By prime factorisation, we get  
 $9604 = \underline{2 \times 2} \times \underline{7 \times 7} \times \underline{7 \times 7}$   
 $\therefore \sqrt{9604} = 2 \times 7 \times 7$   
 $= 98$

2	9604
2	4802
7	2401
7	343
7	49
7	7
	1

(vii) By prime factorisation, we get  
 $5929 = \underline{7 \times 7} \times \underline{11 \times 11}$   
 $\therefore \sqrt{5929} = 7 \times 11$   
 $= 77$

7	5929
7	847
11	121
11	11
	1



(viii) By prime factorisation, we get

$$9216 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \\ \times \underline{3 \times 3}$$

$$\therefore \sqrt{9216} = 2 \times 2 \times 2 \times 2 \times 2 \times 3 \\ = 96$$

2	9216
2	4608
2	2304
2	1152
2	576
2	288
2	144
2	72
2	36
2	18
3	9
3	3
	1

(ix) By prime factorisation, we get

$$529 = 23 \times 23$$

$$\therefore \sqrt{529} = 23$$

23	529
23	23
	1

(x) By prime factorisation, we get

$$8100 = \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{3 \times 3} \times \underline{5 \times 5}$$

$$\therefore \sqrt{8100} = 2 \times 3 \times 3 \times 5 \\ = 90$$

2	8100
2	4050
3	2025
3	675
3	225
3	75
5	25
5	5
	1

### Ex 6.3 Class 8 Maths Question 5.

For each of the following numbers, find the smallest whole number by which it should be multiplied so as to get a perfect square number. Also find the square root of the square number so obtained.

(i) 252

(ii) 180

(iii) 1008

(iv) 2028

(v) 1458

(vi) 768

#### Solution:

(i) By prime factorisation, we get

$$252 = \underline{2 \times 2} \times \underline{3 \times 3} \times 7$$

It is clear that in order to get a perfect square, one more 7 is required.

So, the given number should be multiplied by 7 to make the product a perfect square.

$\therefore 252 \times 7 = 1764$  is a perfect square.

Thus,  $1764 = \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{7 \times 7}$

$\therefore \sqrt{1764} = 2 \times 3 \times 7 = 42$

2	252
2	126
3	63
3	21
7	7
	1

(ii) By prime factorisation, we get

$$180 = \underline{2 \times 2} \times \underline{3 \times 3} \times 5$$

It is clear that in order to get a perfect square, one more 5 is required.

So, the given number should be multiplied by 5 to make the product a perfect square.

$\therefore 180 \times 5 = 900$  is a perfect square.

Thus,  $900 = \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{5 \times 5}$

$\therefore \sqrt{900} = 2 \times 3 \times 5 = 30$

2	180
2	90
3	45
3	15
5	5
	1

(iii) By prime factorisation, we get

$$1008 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{3 \times 3} \times 7$$

It is clear that in order to get a perfect square, one more 7 is required.

So, the given number should be multiplied by 7 to make the product a perfect square.

$$\therefore 1008 \times 7 = 7056 \text{ is a perfect square.}$$

$$\text{Thus, } 7056 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{7 \times 7}$$

$$\begin{aligned} \therefore \sqrt{7056} &= 2 \times 2 \times 3 \times 7 \\ &= 84 \end{aligned}$$

2	1008
2	504
2	252
2	126
3	63
3	21
7	7
	1

(iv) By prime factorisation, we get

$$2028 = \underline{2 \times 2} \times 3 \times \underline{13 \times 13}$$

It is clear that in order to get a perfect square, one more 3 is required.

So, the given number should be multiplied by 3 to make the product a perfect square.

$$\therefore 2028 \times 3 = 6084$$

$$\text{Thus, } 6084 = \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{13 \times 13}$$

$$\therefore \sqrt{6084} = 2 \times 3 \times 13 = 78$$

2	2028
2	1014
3	507
13	169
13	13
	1

(v) By prime factorisation, we get

$$1458 = 2 \times \underline{3 \times 3} \times \underline{3 \times 3} \times \underline{3 \times 3}$$

It is clear that in order to get a perfect square, one more 2 is required.

So, the given number should be multiplied by 2 to make the product a perfect square.

$$\therefore 1458 \times 2 = 2916$$

$$\text{Thus, } 2916 = \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{3 \times 3} \times \underline{3 \times 3}$$

$$\begin{aligned} \therefore \sqrt{2916} &= 2 \times 3 \times 3 \times 3 \\ &= 54 \end{aligned}$$

2	1458
3	729
3	243
3	81
3	27
3	9
3	3
	1

(vi) By prime factorisation, we get

$$768 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times 3$$

It is clear that in order to get a perfect square, one more 3 is required.

So, the given number should be multiplied by 3 to make the product a perfect square.

$$\therefore 768 \times 3 = 2304$$

$$\text{Thus, } 2304 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{3 \times 3}$$

$$\begin{aligned} \therefore \sqrt{2304} &= 2 \times 2 \times 2 \times 2 \times 3 \\ &= 48 \end{aligned}$$

2	768
2	384
2	192
2	96
2	48
2	24
2	12
2	6
3	3
	1

### Ex 6.3 Class 8 Maths Question 6.

For each of the following numbers. find the smallest whole number by which it should be divided so as to get a perfect square. Also find the square root of the square number so obtained.

(i) 252

(ii) 2925

(iii) 396

(iv) 2645

(v) 2800

(vi) 1620

#### Solution:

(i) By prime factorisation, we get

$$252 = \underline{2} \times \underline{2} \times \underline{3} \times \underline{3} \times 7$$

Since the factor 7 cannot be paired.

∴ The given number should be divided by 7.

$$\therefore \frac{252}{7} = \frac{2 \times 2 \times 3 \times 3 \times 7}{7}$$

$$= \underline{2} \times \underline{2} \times \underline{3} \times \underline{3}$$

= 36 is a perfect square

and,  $\sqrt{36} = \sqrt{\underline{2} \times \underline{2} \times \underline{3} \times \underline{3}}$

$$= 2 \times 3 = 6$$

2	252
2	126
3	63
3	21
7	7
	1

(ii) By prime factorisation, we get

$$2925 = \underline{3} \times \underline{3} \times \underline{5} \times \underline{5} \times 13$$

Since the prime factor 13 cannot be paired.

∴ The given number should be divided by 13.

$$\therefore \frac{2925}{13} = \frac{3 \times 3 \times 5 \times 5 \times 13}{13}$$

$$= \underline{3} \times \underline{3} \times \underline{5} \times \underline{5}$$

= 225 is a perfect square

and,  $\sqrt{225} = \sqrt{\underline{3} \times \underline{3} \times \underline{5} \times \underline{5}} = 3 \times 5 = 15$

3	2925
3	975
5	325
5	65
13	13
	1

(iii) By prime factorisation, we get

$$396 = \underline{2 \times 2} \times \underline{3 \times 3} \times 11$$

Since the prime factor 11 cannot be paired.

∴ The given number should be divided by 11.

$$\therefore \frac{396}{11} = \frac{2 \times 2 \times 3 \times 3 \times 11}{11}$$

$$= \underline{2 \times 2} \times \underline{3 \times 3}$$

= 36 is a perfect square

and,  $\sqrt{36} = \sqrt{2 \times 2 \times 3 \times 3} = 2 \times 3 = 6$

2	396
2	198
3	99
3	33
11	11
	1

(iv) By prime factorisation, we get

$$2645 = 5 \times \underline{23} \times \underline{23}$$

Since the prime factor 5 cannot be paired.

∴ The given number should be divided by 5.

$$\therefore \frac{2645}{5} = \frac{5 \times 23 \times 23}{5}$$

= 23 × 23 = 529 is a perfect square

and,  $\sqrt{529} = \sqrt{23 \times 23} = 23$

5	2645
23	529
23	23
	1

(v) By prime factorisation, we get

$$2800 = \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{5 \times 5} \times 7$$

Since the prime factor 7 cannot be paired.

∴ The given number should be divided by 7.

$$\therefore \frac{2800}{7} = \frac{2 \times 2 \times 2 \times 2 \times 5 \times 5 \times 7}{7}$$

$$= \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{5 \times 5}$$

= 400 is a perfect square

and,  $\sqrt{400} = \sqrt{2 \times 2 \times 2 \times 2 \times 5 \times 5} = 2 \times 2 \times 5 = 20$

2	2800
2	1400
2	700
2	350
5	175
5	35
7	7
	1

(vi) By prime factorisation, we get

$$1620 = \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{3 \times 3} \times 5$$

Since the prime factor 5 cannot be paired.

∴ The given number should be divided by 5.

$$\therefore \frac{1620}{5} = \frac{2 \times 2 \times 3 \times 3 \times 3 \times 3 \times 5}{5}$$

$$= \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{3 \times 3}$$

= 324 is a perfect square

and,  $\sqrt{324} = \sqrt{2 \times 2 \times 3 \times 3 \times 3 \times 3}$

$$= 2 \times 3 \times 3 = 18$$

2	1620
2	810
3	405
3	135
3	45
3	15
5	5
	1

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## Chapter - 6

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### Exercise - 6.3

Q7. The students of Class VIII of a school donated ₹2401 in all, for Prime Minister's National Relief Fund. Each student donated as many rupees as the number of students in the class. Find the number of students in the class.

Sol. Let the number of students =  $x$   
Each student donate Rs  $\Rightarrow x \times x$   
Total money contributed by the class VIII  $\Rightarrow$

$$\Rightarrow 2401 = x \times x$$

7	2401
7	343
7	49
7	7
	1

$$2401 = x^2$$

$$x = \sqrt{2401}$$

$$x = \sqrt{7 \times 7 \times 7 \times 7}$$

$$x = 7 \times 7, \quad x = 49$$

The number of students = 49.

Q8. 2025 plants are to be planted in a garden in such a way that each row contains as many plants as the number of rows. Find the number of rows and the number of plants in each row.

Sol. Let the number of rows be  $x$ ,  
the number of plants in each row =  $x$

$$\text{Total number of plants} = 2025$$

$$2025 = x \times x$$

$$x = 3 \times 3 \times 5$$

$$2025 = x^2$$

$$x = 45$$

$$x = \sqrt{2025}$$

$$x = \sqrt{3 \times 3 \times 3 \times 3 \times 5 \times 5}$$

3	2025
3	675
3	225
3	75
5	25
5	5
	1

Q9. Find the smallest square number that is divisible by each of the numbers 4, 9 and 10.

Sol.

2	4, 9, 10
2	2, 9, 5
3	1, 9, 5
3	1, 3, 5
5	1, 1, 5
	1, 1, 1

$\Rightarrow 2 \times 2 \times 3 \times 3 \times 5 \Rightarrow 180$

Here 5 cannot be paired. We will multiply 180 by 5 to get perfect square.  $180 \times 5 = 900$

So the smallest square number divisible by 4, 9 and 100 = 900.

Q10. Find the smallest square number that is divisible by each of the numbers 8, 15 and 10.

Sol.

2	8, 15, 10
2	4, 15, 5
2	2, 15, 5
3	1, 15, 5
5	1, 5, 5
	1, 1, 1

$\Rightarrow 2 \times 2 \times 2 \times 3 \times 5 = 120$

Here 1, 3, 5 and 2 cannot be paired. We will multiply 120 by  $(2 \times 3 \times 5)$  to get perfect square.  $120 \times 30 = 3600$

So the smallest square number divisible by 8, 15 and 10 = 3600.

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Chapter - 6

Ex - 6.4

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Q1. Find the square root of each of the following numbers by Division method.

(i) 2304

Sol.

	4	<u>2304</u>
	+4	16 ↓↓
88		704
+8		704
96		0

82

x 2

164

688

x 8

704

$\sqrt{2304} = 48$

(iii) 3481

	5	<u>3481</u>
	+5	25 ↓↓
109		981
+9		981
118		0

$\sqrt{3481} = 59$

(ii) 4489

	6	<u>4489</u>
	+6	36 ↓↓
127		889
+7		889
134		0

123

x 3

369

127

x 7

889

$\sqrt{4489} = 67$

(iv) 529

	2	<u>529</u>
	+2	4 ↓↓
43		129
+3		129
46		0

$\sqrt{529} = 23$



3249

	57
5	3249
+5	25
107	749
+7	749
114	0

$\sqrt{3249} = 57$

(viii) 7921

	89
8	7921
+8	64
169	1521
+9	1521
178	0

$\sqrt{7921} = 89$

(vii) 1369

	37
3	1369
+3	9
67	469
+7	469
74	0

$\sqrt{1369} = 37$

(ix) 576

	24
2	576
+2	4
44	176
+4	176
48	0

$\sqrt{576} = 24$

(x) 1024

	32
3	1024
+3	9
62	124
+2	124
64	0

$\sqrt{1024} = 32$

(vi) 5776

	76
7	5776
+7	49
146	876
+6	876
152	0

$\sqrt{5776} = 76$

(xi)  $\sqrt{3136}$

$$\begin{array}{r} 56 \\ 5 \overline{) 3136} \\ \underline{+5} \phantom{00} 25 \phantom{00} \\ 106 \phantom{00} 636 \\ \underline{+6} \phantom{00} 636 \\ 112 \phantom{00} 0 \end{array}$$

$\sqrt{3136} = 56$

(xii)  $\sqrt{900}$

$$\begin{array}{r} 30 \\ 3 \overline{) 900} \\ \underline{+3} \phantom{00} 900 \\ 60 \phantom{00} 000 \end{array}$$

$\sqrt{900} = 30$

Q2. Find the number of digits in the square root of each of the following numbers (with any calculation)

(i)  $\sqrt{64}$   
even  
 $\frac{n}{2} = \frac{2}{2} = 1$   
64 contains two digit which is even.

(ii)  $\sqrt{144}$   
odd  
 $\frac{n+1}{2} = \frac{3+1}{2} = 2$   
144 contains 3 digit which is odd.

(iii)  $\sqrt{4489}$   
 $\frac{n}{2} = \frac{4}{2} = 2$   
4489 contains 4 digit which is even.

(iv)  $\sqrt{27225}$   
 $\frac{n+1}{2} = \frac{5+1}{2} = 3$   
27225 contains 5 digit which is odd.

390625

390625 Contains 6 digit which is even.

$$\frac{n}{2} = \frac{6}{2} = 3.$$

Find the square root of the following decimal numbers:-

(i) 2.56

(ii) 7.29

	1.6	
1	2.56	
+1	1 ↓↓	
26	156	
+6	156	
32	0	

	2.7	
2	7.29	
+2	4 ↓↓	
47	329	
+7	329	
54	0	

$$\sqrt{2.56} = 1.6$$

$$\sqrt{7.29} = 2.7$$

(iii) 51.84

(iv) 42.25

(v) 31.36

	7.2	
7	51.84	
+7	49 ↓↓	
142	284	
+2	284	
146	0	

	6.5	
6	42.25	
+6	36 ↓↓	
125	625	
+5	625	
130	0	

	5.6	
5	31.36	
+5	25 ↓↓	
106	636	
+6	636	
112	0	

$$\sqrt{51.84} = 7.2$$

$$\sqrt{42.25} = 6.5$$

$$\sqrt{31.36} = 5.6$$

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Q4. Find the least number which must be subtracted from each of the following numbers so as to get a perfect square. Also find the square root of the perfect square root of the perfect square so obtained.

(i) 402

$$\begin{array}{r} 2 \\ \hline 2 \overline{) 402} \\ + 2 \quad 4 \cancel{0} \cancel{2} \\ \hline 4 \quad 0 \quad 0 \quad 2 \end{array}$$

We must subtract 2 from 402 to get a perfect square.  
New number =  $402 - 2 = 400$

$$\begin{array}{r} 20 \\ \hline 2 \overline{) 400} \\ + 2 \quad 4 \cancel{0} \cancel{0} \\ \hline 40 \quad 0 \quad 0 \end{array}$$

$$\sqrt{400} = 20.$$

(ii) 1989

$$\begin{array}{r} 44 \\ \hline 4 \overline{) 1989} \\ + 4 \quad 16 \cancel{8} \cancel{9} \\ \hline 84 \quad 3 \quad 8 \quad 9 \\ 4 \quad 3 \quad 3 \quad 6 \\ \hline 88 \quad 5 \quad 3 \end{array}$$

$$\begin{array}{r} 44 \\ \hline 4 \overline{) 1936} \\ + 4 \quad 16 \cancel{3} \cancel{6} \\ \hline 84 \quad 3 \quad 3 \quad 6 \\ + 4 \quad 3 \quad 3 \quad 6 \\ \hline 88 \quad 0 \end{array}$$

$$\sqrt{1936} = 44.$$

We must subtract 53 from 1989 to get a perfect square.

$$\text{New number} = 1989 - 53 = 1936$$

ted  
to get  
of  
are

$$\begin{array}{r}
 \text{(iii)} \quad 3250 \\
 \quad \quad 57 \\
 \hline
 5 \overline{) 3250} \\
 + 5 \quad 25 \downarrow \downarrow \\
 \hline
 107 \quad 750 \\
 + 7 \quad 749 \\
 \hline
 114 \quad 1
 \end{array}$$

$$\begin{array}{r}
 \quad \quad 57 \\
 \hline
 5 \overline{) 3249} \\
 + 5 \quad 25 \downarrow \downarrow \\
 \hline
 107 \quad 749 \\
 + 7 \quad 749 \\
 \hline
 114 \quad 0 \\
 \hline
 \sqrt{3249} = 57.
 \end{array}$$

We must subtract 1 from 3250 to get a perfect square. New number =  $3250 - 1 = 3249$ .

to

$$\begin{array}{r}
 \text{(iv)} \quad 825 \\
 \quad \quad 2 \\
 \hline
 2 \overline{) 825} \\
 + 2 \quad 4 \downarrow \downarrow \\
 \hline
 48 \quad 425 \\
 + 8 \quad 384 \\
 \hline
 56 \quad 41
 \end{array}$$

$$\begin{array}{r}
 \quad \quad 28 \\
 \hline
 2 \overline{) 784} \\
 + 2 \quad 4 \downarrow \downarrow \\
 \hline
 48 \quad 384 \\
 + 8 \quad 384 \\
 \hline
 56 \quad 0 \\
 \hline
 \sqrt{784} = 28.
 \end{array}$$

We must subtract 41 from 825 to get a perfect square. New number =  $825 - 41 = 784$ .

$$\begin{array}{r}
 \text{(v)} \quad 4000 \\
 \quad \quad 6 \\
 \hline
 6 \overline{) 4000} \\
 + 6 \quad 36 \downarrow \downarrow \\
 \hline
 123 \quad 400 \\
 + 3 \quad 369 \\
 \hline
 126 \quad 31
 \end{array}$$

$$\begin{array}{r}
 \quad \quad 63 \\
 \hline
 6 \overline{) 3969} \\
 + 6 \quad 36 \downarrow \downarrow \\
 \hline
 123 \quad 369 \\
 + 3 \quad 369 \\
 \hline
 126 \quad 0 \\
 \hline
 \sqrt{3969} = 126.
 \end{array}$$

We must subtract 31 from 4000 to get a perfect square. New number =  $4000 - 31 = 3969$ .

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$826 - 6.4$

Q5. Find the least number which must be added to each of the following numbers so as to get a perfect square. Also find the square root of the perfect square so obtained.

(i) 525

23	22
23	22
69	42
67	42
29	44
25	44
04	

	23
2	529
+2	4
43	129
+3	129
46	0

$\sqrt{529} = 23$

Here  $(22)^2 < 525 < (23)^2$   
 so if we add 4 to 525, it will be perfect square.  
 New number =  $525 + 4 = 529$ .

(ii) 1750

	41
4	1750
+4	16
81	150
+1	81
82	69

	42
4	1750
+4	16
82	150
+2	164

	42
4	1764
+4	16
82	164
+2	164
84	0

Here  $(42)^2 < 1750 < (42)^2$

We can say 1750 is  $(164 - 150) = 14$  less than  $(42)^2$

so if we add 14 to 1750, it will be perfect square.  
 New no. =  $1750 + 14 = 1764$       $\sqrt{1764} = 42$ .

(iii) 252

$$\begin{array}{r}
 15 \\
 \hline
 1 \overline{) 252} \\
 +1 \downarrow \\
 \hline
 25 \overline{) 152} \\
 +5 \downarrow \\
 \hline
 30 \overline{) 27}
 \end{array}$$

$$\begin{array}{r}
 16 \\
 \hline
 1 \overline{) 256} \\
 +1 \downarrow \\
 \hline
 26 \overline{) 156} \\
 +6 \downarrow \\
 \hline
 32 \overline{) 0}
 \end{array}$$

Here  $(15)^2 < 252 > (16)^2$

So if we add 4 to 252, it will be perfect square.  
New number =  $252 + 4 = 256$ .

$$\sqrt{256} = 16.$$

(iv) 1825

$$\begin{array}{r}
 42 \\
 \hline
 4 \overline{) 1825} \\
 +4 \downarrow \\
 \hline
 82 \overline{) 225} \\
 +2 \downarrow \\
 \hline
 84 \overline{) 63}
 \end{array}$$

$$\begin{array}{r}
 43 \\
 \hline
 4 \overline{) 1849} \\
 +4 \downarrow \\
 \hline
 83 \overline{) 249} \\
 +3 \downarrow \\
 \hline
 86 \overline{) 0}
 \end{array}$$

Here  $(42)^2 < 1825 > (43)^2$

So if we add 24 to 1825, it will be perfect square number

New number  $\Rightarrow 1825 + 24 \Rightarrow 1849$

$$\sqrt{1849} = 43.$$

(v) 6412

$$\begin{array}{r}
 80 \\
 8 \overline{) 6412} \\
 + 8 \quad 64 \downarrow \downarrow \\
 \hline
 160 \quad 0 \quad 120
 \end{array}$$

$$\begin{array}{r}
 81 \\
 8 \overline{) 6561} \\
 + 8 \quad 64 \downarrow \downarrow \\
 \hline
 161 \quad 16 \downarrow \\
 + 1 \quad 161 \\
 \hline
 162 \quad 0
 \end{array}$$

$$\begin{array}{r}
 81 \\
 \times 81 \\
 \hline
 81 \\
 648 \phantom{x} \\
 \hline
 6561 \\
 - 6412 \\
 \hline
 0149
 \end{array}$$

Here  $(80)^2 < 6412 < (81)^2$

So if we add  $6412 + 149$ , it will be perfect square

New number = 6561

$$\sqrt{6561} = 81$$



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Q6. Find the length of the side of a square whose area is  $441 \text{ m}^2$ .

Sol. Let the length of each side of the square =  $a$ .  
Then area of square  $\Rightarrow a \times a = (a)^2$ .

$$a^2 = 441 \text{ m}^2$$

$$a = \sqrt{441}$$

$$\begin{array}{r|l} 21 & 441 \\ +2 & 4 \\ \hline 41 & 041 \\ 1 & 41 \\ \hline 42 & 0 \end{array}$$

$$\sqrt{441} = 21$$

The length of each side of the square =  $a = 21 \text{ m}$ .

Q7. In a right triangle ABC,  $\angle B = 90^\circ$ .

(a) If  $AB = 6 \text{ cm}$ ,  $BC = 8 \text{ cm}$ , find  $AC$ .

Sol. Given =  $AB = 6 \text{ cm}$ ,  $BC = 8 \text{ cm}$ .  
Let  $AC$  be  $x \text{ cm}$ .

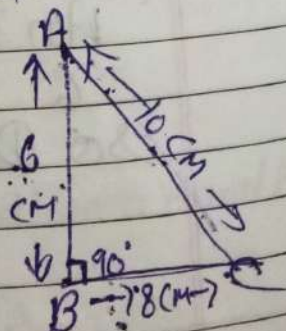
$$AC^2 = AB^2 + BC^2$$

$$AC^2 = (6)^2 + (8)^2$$

$$AC^2 = 36 + 64$$

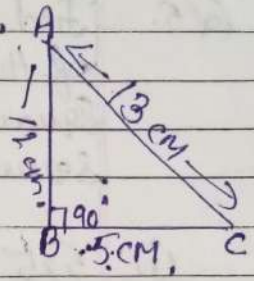
$$AC^2 = 100$$

$$AC = \sqrt{100} \Rightarrow 10, \quad AC = 10.$$



B. If  $Ac = 13 \text{ cm}$ ,  $Bc = 5 \text{ cm}$ , find  $AB$ .

Sol Given  $Ac = 13 \text{ cm}$ ,  $Bc = 5 \text{ cm}$ .  
Let  $AB$  be  $x \text{ cm}$ .



$$\begin{aligned} (AB)^2 &= (AC)^2 - (BC)^2 \\ (AB)^2 &= (13)^2 - (5)^2 \\ (AB)^2 &= 169 - 25 \\ (AB)^2 &= 144 \\ AB &= \sqrt{144} \Rightarrow 12 \text{ cm.} \end{aligned}$$

Q8. A gardener has 1000 plants. He wants to plant these in such a way that the number of rows and the number of columns remain same. Find the minimum number of plants he needs more for this.

Sol Let the number of rows and column be  $x$ .  
Total no. of row and column  $= x \times x = x^2$   
 $x^2 = 1000$ ,  $x = \sqrt{1000}$

31	3   1000	32	3   1000
+3	9 ↓ ↓	+3	9 ↓ ↓
61	7 0 0	62	1 0 0
+3	6 1	+2	1 2 4
62	3 9	or	.

we can say 1000 is  
 $(124 - 100)^2 = 24$   
less than  $(32)^2$ .

Here  $(31)^2 < 1000 > (32)^2$   
So if we add 24 to 1000 we get perfect square no.  
New number  $= 1000 + 24 = 1024$   
24 more plants are needed.

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Q9. There are 500 children in a school. For a P.T drill they have to stand in such a manner that the number of rows is equal to number of columns. How many children would be left out in this arrangement.

Sol. Let the number of rows and column be  $=x$ .  
Total number of row and column  $=x \times x = x^2$   
 $x^2 = 500$   
 $x = \sqrt{500}$

$$\begin{array}{r|l} 22 & 500 \\ \hline 9 & \overline{500} \\ +2 & 400 \\ \hline 42 & 100 \\ +2 & 84 \\ \hline 44 & 16 \end{array}$$

So, 16 children would be left out in the arrangement.